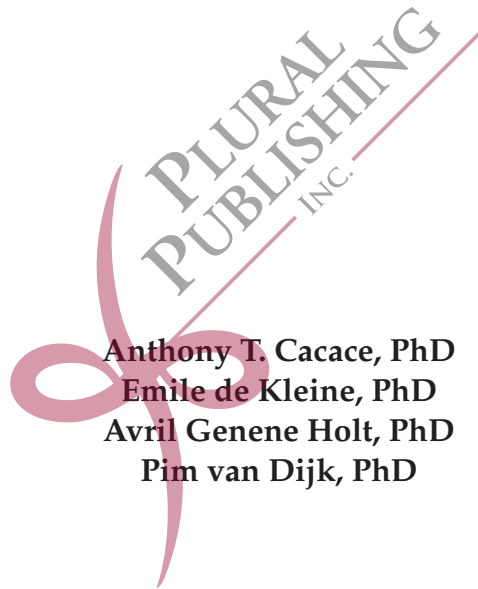


# Scientific Foundations of Audiology

*Perspectives from Physics, Biology,  
Modeling, and Medicine*



Anthony T. Cacace, PhD  
Emile de Kleine, PhD  
Avril Genene Holt, PhD  
Pim van Dijk, PhD



# CONTENTS

<i>Introduction</i>	<i>vii</i>
<i>Contributors</i>	<i>ix</i>
<b>1</b> Middle-Ear Reflectance: Concepts and Clinical Applications <i>Jont B. Allen, Sarah R. Robinson, Judi A. Lapsley Miller, Patricia S. Jeng, and Harry Levitt</i>	1
<b>2</b> Otoacoustic Emissions: Measurement, Modeling, and Applications <i>Glenis Long and Bastian Epp</i>	41
<b>3</b> The Audiogram: What It Measures, What It Predicts, and What It Misses <i>Anthony T. Cacace and Robert F. Burkard</i>	57
<b>4</b> Contemporary Issues in Vestibular Assessment <i>Faith W. Akin, Owen D. Murnane, and Kristal Mills Riska</i>	73
<b>5</b> Genetics of Deafness: In Mice and Men <i>Mirna Mustapha and Avril Genee Holt</i>	99
<b>6</b> Molecular-Based Measures for the Development of Treatment for Auditory System Disorders: Important Transformative Steps Toward the Treatment of Tinnitus <i>Avril Genee Holt, Catherine A. Martin, Antonela Muca, Angela R. Dixon, and Magnus Bergkvist</i>	107
<b>7</b> Medical and Surgical Treatment of Inner Ear Disease <i>Lawrence R. Lustig</i>	131
<b>8</b> The Future of Cochlear Implants <i>Richard Tyler, Paul R. Kileny, Aniruddha K. Deshpande, Shruti Balvalli Deshpande, Camille Dunn, Marlan Hansen, and Bruce Gantz</i>	175
<b>9</b> Novel Approaches for Protection and Restoration of Hearing <i>Min Young Lee and Yehoash Raphael</i>	197
<b>10</b> The Olivocochlear System: A Current Understanding of Its Molecular Biology and Functional Roles in Development and Noise-Induced Hearing Loss <i>Douglas E. Vetter</i>	219

<b>11</b>	Current Progress With Auditory Midbrain Implants <i>Hubert H. Lim, James F. Patrick, and Thomas Lenarz</i>	255
<b>12</b>	Perception and Psychoacoustics of Speech in Cochlear Implant Users <i>Deniz Başkent, Etienne Gaudrain, Terrin Nichole Tamati, and Anita Wagner</i>	285
<b>13</b>	Theoretical Considerations in Developing an APD Construct: A Neuroscience Perspective <i>Dennis J. McFarland and Anthony T. Cacace</i>	321
<b>14</b>	Normal Sound Processing: fMRI <i>Stefan Uppenkamp and Roy D. Patterson</i>	331
<b>15</b>	Tinnitus Neurophysiology According to Structural and Functional Magnetic Resonance Imaging <i>Dave R. M. Langers and Emile de Kleine</i>	351
	<i>Index</i>	371



# INTRODUCTION

This is not your typical textbook in audiology; rather, it represents a compendium of state-of-the-art chapters on unique topics dealing with hearing, vestibular, and brain science, the majority of which are not found in standard texts but are highly pertinent to the field. The underlying theme is that audiology is the primary “translational interface” between basic science and clinical concerns. Trained primarily as clinicians and clinical scientists, audiologists are situated in a unique position to implement breakthroughs in engineering, molecular biology, neuroimaging, genetics, medicine, nanobioscience, etc., and deliver them to the clinic. However, the underlying advancements require a fundamental understanding of advanced concepts and materials. Therefore, our intent is to provide a foundation for doctoral students in audiology, physics, neurobiology, and engineering and residents in various medical specialties (otolaryngology, neurology, pediatrics, and neurosurgery) with the background and concepts necessary to facilitate understanding in these different areas.

Of the “Current issues” subsumed within this book, we focus on topics that have practical, experimental, and theoretical value. The practical information is clearly apparent and is directly applicable to clinical situations. However, within this material, we also provide insight into basic areas of research where technical information is developing, where our understanding is incomplete, where theory has *not* been applied in a rigorous manner, and where exper-

imental models can be improved upon to validate our concepts in complex areas. We hope that the end result will inspire new investigators to fill in the gaps and advance the field.

Moreover, it should be obvious that after viewing the table of contents, the topics being covered are expansive. They range from areas of basic science (anatomy, physiology, genetics, gene expression, molecular biology, neurochemistry) and clinical concerns (peripheral and central otopathology) to other relevant domains in assessment and treatment. They cover physical principles of middle ear and inner ear function (auditory, vestibular, balance), molecular and neural substrate underlying normal and pathologic activity in afferent and efferent pathways, implanted devices (cochlear and mid-brain implants), mechanisms of speech perception associated with electrical stimulation, to the cortical processing of sound (normal and pathological) using noninvasive methods vis-à-vis magnetic resonance imaging (MRI).

We also consider “Future perspectives” in a similar context to those areas described above. However, these particular areas will no doubt be transformative in nature, where advancements are motivated by the ingenuity of the investigators and where the potential to produce large dividends (successful treatments and potential cures) is on the horizon. One area of interest concerns the combined use of manganese-enhanced MRI (MEMRI), gene expression, and functionalized nanoparticles

to treat noise-induced tinnitus. Another very exciting domain concerns novel approaches for the protection and restoration of hearing. This highly fluid area is expected to have substantial impact on the field, where future developments remain extremely bright.

It is our hope that information derived from these topics expands one's knowledge base but also provides the incentive to improve the status quo. However, this is not an easy task. To succeed in this ambitious undertaking, we have assembled a stellar array of international world-class scientists, clinicians, and scholars to ensure that state-of-the-art technical information is explicated in an understandable, logical, and cohesive manner. The authors of these chapters have taken this task very seriously and share the common responsibility for giving an expose on potential gaps in knowledge that currently exist in a thoughtful and unselfish manner. We are extremely grateful for their efforts and contributions.

To summarize, we believe that this book will have many beneficiaries. They will be independent of geographical boundaries but will have in common the desire to learn and apply new and advanced concepts to everyday situations. This includes a broad spectrum of individuals from multiple scientific disciplines, including medicine (otolaryngology, pediatrics, neurology,

neurosurgery), engineering (biomedical, mechanical, electrical, chemical), basic science (neuro/molecular biology and neurochemistry), rehabilitation, physics, psychology, and of course audiology, where each group will have specific domains-of-interest and applications. We also believe that having a literary source in one book that contains a repository of diverse and highly technical information, presented in a coherent manner, should be extremely valuable to a wide range of individuals, but to our knowledge, such a document does *not* yet exist. Therefore, this book should fill an important void in the scientific literature as a combined reference text, research guide, and educational tool.

As science in this area evolves, the profession of audiology is in a unique position to integrate advanced technologies developed by clinicians, engineers, and basic scientists and apply them to the clinic. Consequently, audiologists and others in related fields like medicine and engineering represent the "translational interface" between basic science and current clinical concerns. It is a big responsibility to integrate new ideas and concepts into the clinic but it is one that encompasses the technical skills and educational background of those individuals already working in this field.

# CONTRIBUTORS

**Faith W. Akin, PhD**

Vestibular/Balance Laboratory  
Mountain Home VA Medical Center  
Professor  
Department of Audiology and  
Speech-Language Pathology  
East Tennessee State University  
Mountain Home, Tennessee  
*Chapter 4*

**Jont B. Allen, PhD**

Professor  
Department of Computer and  
Electrical Engineering  
University of Illinois  
Urbana, Illinois  
*Chapter 1*

**Deniz Baskent, PhD, MSc**

Professor  
Department of Otorhinolaryngology-  
Head and Neck Surgery  
University of Groningen  
University Medical Center Groningen  
Research School of Behavioral and  
Cognitive Neurosciences  
Groningen, The Netherlands  
*Chapter 12*

**Magnus Bergkvist, PhD**

Assistant Professor of Nanobioscience  
SUNY Polytechnic Institute  
Colleges of Nanoscale Science and  
Engineering  
Albany, New York  
*Chapter 6*

**Robert F. Burkard, PhD, CCC-A**

Professor and Chair

Department of Rehabilitation  
Science  
University at Buffalo  
Buffalo, New York  
*Chapter 3*

**Anthony T. Cacace, PhD**

Professor and Director of the Hearing  
Science Laboratory  
Department of Communication  
Sciences & Disorders  
Wayne State University  
Detroit, Michigan  
*Chapters 3 and 13*

**Emile de Kleine, PhD**

Medical Physicist-Audiologist  
University of Groningen  
University Medical Center Groningen  
Groningen, The Netherlands  
*Chapter 15*

**Aniruddha K. Deshpande, PhD,  
CCC-A**

Assistant Professor  
Department of Speech-Language-  
Hearing Sciences  
Hofstra University  
Hempstead, New York  
*Chapter 8*

**Shruti Balvalli Deshpande, PhD,  
CCC-A**

Visiting Assistant Professor  
Postdoctoral Research Scholar  
The University of Iowa  
Iowa City, Iowa  
*Chapter 8*

**Angela R. Dixon, PhD**  
Postdoctoral Fellow  
Department of Anatomy and Cell  
Biology  
Molecular Anatomy of Central  
Auditory Related Systems  
Wayne State University School of  
Medicine  
Detroit, Michigan  
*Chapter 6*

**Camille Dunn, PhD**  
Research Assistant Professor  
Department of Otolaryngology  
University of Iowa  
Iowa City, Iowa  
*Chapter 8*

**Bastian Epp, Dr. Rer. Nat.**  
Assistant Professor  
Hearing Systems Group  
Department of Electrical Engineering  
Technical University of Denmark  
Lyngby, Denmark  
*Chapter 2*

**Bruce Gantz, MD**  
Professor and Chair  
Department of Otolaryngology  
University of Iowa  
Iowa City, Iowa  
*Chapter 8*

**Etienne Gaudrain, PhD, MSc**  
Senior Researcher  
Lyon Neuroscience Research Center  
Auditory Cognition and  
Psychoacoustics Team  
Department of Otorhinolaryngology-  
Head and Neck Surgery  
University of Groningen  
University Medical Center Groningen  
Research School of Behavioral and  
Cognitive Neurosciences

Groningen, The Netherlands  
*Chapter 12*

**Marlan Hansen, MD**  
Associate Professor  
Department of Otolaryngology  
University of Iowa  
Iowa City, Iowa  
*Chapter 8*

**Avril Genene Holt, PhD**  
Associate Professor  
Department of Anatomy and Cell  
Biology  
Molecular Anatomy of Central  
Auditory Related Systems  
Wayne State University School of  
Medicine  
Health Science Specialist  
John D. Dingell VA Medical Center  
Detroit, Michigan  
*Chapters 5 and 6*

**Patricia S. Jeng, PhD**  
Mimosa Acoustics, Inc.  
Mahomet, Illinois  
*Chapter 1*

**Paul R. Kileny, PhD**  
Professor of Otolaryngology  
Director, Academic  
Program–Audiology  
Department of Otolaryngology-Head  
and Neck Surgery  
University of Michigan Health System  
Ann Arbor, Michigan  
*Chapter 8*

**Dave R. M. Langers, PhD**  
Department of Otorhinolaryngology  
University of Groningen  
University Medical Center Groningen  
Groningen, The Netherlands  
*Chapter 15*

**Min Young Lee, MD**

Kresge Hearing Research Institute  
 Department of Otolaryngology-Head  
 and Neck Surgery  
 University of Michigan Medical  
 School

Ann Arbor, Michigan

*Chapter 9*

**Thomas Lenarz, MD, PhD**

Professor and Director  
 Department of Otolaryngology  
 Hannover Medical School  
 Hannover, Germany

*Chapter 11*

**Harry Levitt, BSc, PhD**

Professor Emeritus  
 The City University of New York  
 Director of Research  
 Advanced Hearing Concepts  
 Bodega Bay, California

*Chapter 1*

**Hubert H. Lim, PhD**

Assistant Professor  
 Biomedical Engineering and  
 Otolaryngology  
 Institute for Translational  
 Neuroscience Scholar

University of Minnesota, Twin Cities  
 Minneapolis, Minnesota

*Chapter 11*

**Glenis Long, PhD**

CUNY Graduate Center  
 Professor Emerita  
 Speech-Language-Hearing Science  
 Program

New York, New York

*Chapter 2*

**Lawrence R. Lustig, MD**

Howard W. Smith Professor and Chair

Department of Otolaryngology-Head  
 and Neck Surgery

Columbia University Medical Center  
 New York, New York

*Chapter 7*

**Catherine A. Martin, BA**

Kresge Hearing Research Institute  
 University of Michigan

Ann Arbor, Michigan

*Chapter 6*

**Dennis J. McFarland, PhD**

Research Scientist  
 National Center for Adaptive  
 Neurotechnologies

Wadsworth Center  
 New York State Department of  
 Health

Albany, New York

*Chapter 13*

**Judi A. Lapsley Miller, PhD**

Senior Scientist  
 Mimosa Acoustics, Inc.  
 Hearing Research Consultant  
 Wellington, New Zealand

*Chapter 1*

**Antonela Muca**

Wayne State University School of  
 Medicine

Detroit, Michigan

*Chapter 6*

**Owen D. Murnane, PhD**

Vestibular/Balance Laboratory  
 Mountain Home VA Medical Center  
 Professor

Department of Audiology and  
 Speech-Language Pathology

East Tennessee State University  
 Mountain Home, Tennessee

*Chapter 4*



**Mirna Mustapha, PhD**

Assistant Professor  
Department of Otolaryngology-Head  
and Neck Surgery  
Stanford University School of Medicine  
Stanford, California  
*Chapter 5*

**James F. Patrick, AO, DEng, FTSE,  
FIE (AUST), CPEng (Biomed)**

Chief Scientist, Senior Vice President  
Cochlear Limited  
Adjunct Professor, Macquarie  
University  
Associate Professor, University of  
Melbourne  
Adjunct Professor, LaTrobe University  
Sydney, Australia  
*Chapter 11*

**Roy D. Patterson, PhD**

Professor  
Department of Physiology,  
Development and Neuroscience  
University of Cambridge  
Cambridge, United Kingdom  
*Chapter 14*

**Yehoash Raphael, PhD**

The R. Jamison and Betty Williams  
Professor of Otolaryngology-Head  
and Neck Surgery Kresge Hearing  
Research Institute  
The University of Michigan  
Ann Arbor, Michigan  
*Chapter 9*

**Kristal Mills Riska, AuD, PhD**

Vestibular/Balance Laboratory  
Mountain Home VA Medical Center  
Assistant Professor  
Department of Audiology and  
Speech-Language Pathology  
East Tennessee State University  
Mountain Home, Tennessee  
*Chapter 4*

**Sarah R. Robinson, MS**

PhD Candidate  
Department of Electrical and  
Computer Engineering  
University of Illinois at  
Urbana-Champaign  
Urbana, Illinois  
*Chapter 1*

**Terrin Nichole Tamati, PhD**

Postdoctoral Researcher  
Department of Otorhinolaryngology-  
Head and Neck Surgery  
University of Groningen  
University Medical Center Groningen  
Groningen, The Netherlands  
*Chapter 12*

**Richard Tyler, PhD**

Professor  
Department of Otolaryngology  
University of Iowa  
Iowa City, Iowa  
*Chapter 8*

**Stefan Uppenkamp, PD Dr. Rer. Nat.  
Habil.**

Physicist  
Medical Physics Section  
University of Oldenburg  
Oldenburg, Germany  
*Chapter 14*

**Pim van Dijk, PhD**

Medical Physicist and Audiologist  
University of Groningen  
University Medical Center Groningen  
Groningen, The Netherlands

**Douglas E. Vetter, PhD**

Associate Professor  
Department of Neurobiology and  
Anatomical Sciences  
University of Mississippi  
Jackson, Mississippi  
*Chapter 10*

**Anita Wagner, PhD, MA**  
Researcher  
Department of Otorhinolaryngology-  
Head and Neck Surgery  
University of Groningen

University Medical Center Groningen  
Research School of Behavioral and  
Cognitive Neurosciences  
Groningen, The Netherlands  
*Chapter 12*



*To my AuD and PhD students for their inspiration and interest in science and research, which in part motivated the need for such a book; To those students, scientists, and clinicians who will continue to advance the field; and To my wife Lydia, for her unwavering support.*

—Anthony T. Cacace

*To my wife Margreet and our girls Veerle and Céline.*

—Emile de Kleine

*To my laboratory team for their boundless energy and enthusiasm for science; To my colleagues at Wayne State University and The Kresge Hearing Research Institute, University of Michigan for thought-provoking and stimulating scientific conversations; To my Saline CoC family for helping me to stay grounded; To my parents for giving me a solid foundation and for their continuous encouragement; and To my husband Ron and our son Parker, who through their support, provide me with the opportunity to continue the work I love.*

—Avril Genene Holt

*To my wife Jacqueline and children Jop and Jet; and To my scientific colleagues at the University Medical Center Groningen, University of Groningen, University of Oldenburg, Graduate Center of the City University of New York, University of Tübingen, University of Cambridge and University of California, Los Angeles for great collaborations in the past and at present.*

—Pim van Dijk

# CHAPTER 1

## Middle-Ear Reflectance: Concepts and Clinical Applications

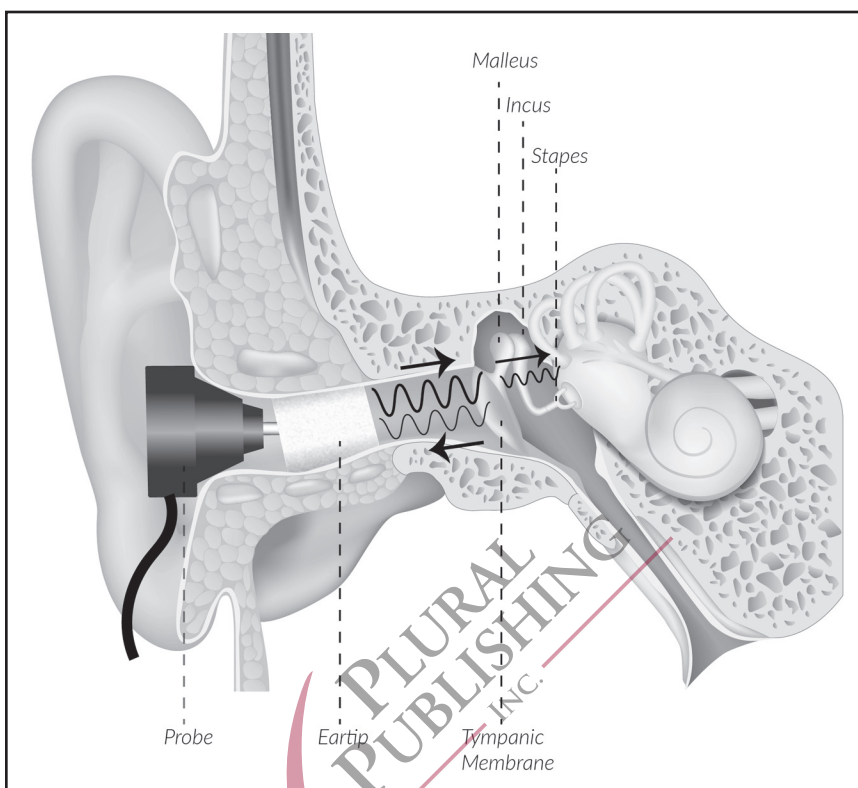
Jont B. Allen, Sarah R. Robinson, Judi A. Lapsley  
Miller, Patricia S. Jeng, and Harry Levitt

The middle ear is a complex sound transmission system that converts airborne sound into cochlear fluid-borne sound, in a relatively efficient way, over the bandwidth of hearing (about 0.1–15 kHz). The middle ear is the gateway to the auditory system, and it is involved in nearly every audiologic test. It is therefore critical to assess middle-ear status in any audiologic evaluation and, in the case of abnormal middle-ear function, pinpoint the source of pathology to enable an appropriate medical intervention. By the use of wideband acoustic measurements, the middle-ear structures can be non-invasively probed across the wide frequency range of hearing, allowing clinicians to make nuanced interpretations of hearing health. The term *wideband acoustic immittance* (WAI) has recently been coined as an umbrella term to identify a variety of acoustic quanti-

ties measured in the ear canal (Feeney et al., 2013). Here we focus primarily on wideband reflectance, from which other WAI quantities may be derived. The *reflectance* is defined as the ratio of reflected to forward pressure waves.

A middle-ear reflectance measurement involves inserting an acoustic measurement probe into the ear canal, fitted with an ear tip designed to create a sealed ear-canal cavity (Figure 1–1). A hearing aid loudspeaker in the probe transmits wideband sound into the ear canal. Any reflected sound, related to structures of the middle ear, is measured by the probe microphone. This probe is calibrated in such a way that the absorbed and reflected pressures in a cavity may be determined.

Reflectance measurements are clinically practical to make: The measurement takes less than a minute and the ear does not require pressurization. The



**Figure 1–1.** Probe configuration in the ear canal to measure middle-ear reflectance, showing the acoustic signal traveling down the ear canal until it reaches the TM. At the TM, the sound is partially reflected back into the ear canal and partially absorbed into the middle ear.

same probe can be used for other audiologic tests, such as otoacoustic emission (OAE) tests and pure-tone hearing threshold testing. Such testing, when a microphone is used in the ear canal, is known as *real-ear* testing. Given knowledge of the reflectance, it is possible to correct for troublesome ear canal standing waves, which can produce large artifacts in the real-ear calibrations. Alone, or together with other audiologic measurements, middle-ear reflectance measurements can help identify many abnormal conditions which may

lead to conductive hearing loss (CHL), including degrees of otitis media, tympanic membrane (TM) perforations, otosclerosis, and ossicular disarticulation. The method is noninvasive, fast, and clinically available.

In this chapter, we cover the theoretical principles of middle-ear reflectance. We then move to clinical applications, showing how normal middle ears behave and how abnormal middle ears differ. We offer advice on how to make quality measurements and provide suggestions for future research.

## Background to Middle-Ear Assessment

---

Noninvasive assessment of middle-ear status is of great importance in hearing health care. An early approach to middle-ear assessment is that of *tympanometry* (e.g., Feldman, 1976; Shanks, 1988), and it is still the clinical gold standard. The method relies on measurements at low frequencies (e.g., probe tones at 226 Hz and 1,000 Hz are commonly used) and provides no information on the status of the middle ear at higher frequencies relevant to speech perception (e.g., 0.2–8.0 kHz). The methods employed in tympanometry were developed prior to the introduction of digital technology, and these methods reflect the limitations of that era.

Reflectance of sound from the TM and the acoustic impedance of the middle ear are different facets of the same underlying mechanism. Historically, acoustic impedance of the ear was the first to be measured and studied (West, 1928). There is a substantial body of research on the acoustic impedance of the ear. Metz (1946) developed the first clinical instrument for measuring the acoustic impedance of the ear. This instrument was not easy to use and clinical measurement of acoustic impedance proceeded at a slow pace until more practical instruments were developed (Møller, 1960; Terkildsen & Nielsen, 1960; Zwislocki & Feldman, 1970). Tympanometry, the measurement of the middle-ear acoustic impedance as a function of static pressure in the ear canal, provided useful clinical data. Thus, practical instruments were developed for measurements of this

type. The 1970s saw a rapid growth in the use of tympanometry, which is widely used today in audiologic evaluations (Jerger, 1970).

The introduction of small, inexpensive computers in the mid-1980s paved the way for a new generation of digital test equipment with capabilities well beyond that of conventional electronic instrumentation. It also facilitated new ways of thinking about audiologic measurement, resulting in the development of innovative wideband techniques. The evolution of wideband reflectance measurement allows for more detailed diagnostic assessment of the middle-ear status than the previous approach based on tympanometry. Early reflectance studies were conducted by Keefe, Ling, and Bulen (1992); Keefe, Bulen, Arehart, and Burns (1993); and Voss and Allen (1994).

The use of reflectance measurements in a computer-based system does not preclude the use of acoustic impedance data, where appropriate. Acoustic reflectance and acoustic impedance are both WAI quantities; different facets of the same underlying mechanism. If one is known, the other can be computed by means of a mathematical transformation. This mathematical transformation can be implemented conveniently in a computer-based instrument.

## Acoustics of the Outer and Middle Ear

---

When a sound wave travels down the ear canal toward the TM, the acoustic power is continuous until it reaches an *impedance discontinuity*, such as the

### Propagation of Sound: The Basics

Many of the concepts in WAI, including reflectance, are defined in mathematical or physics terms. This creates a problem for clinicians and others without the necessary background. Here we explain some acoustical concepts in lay terms.

The transmission of sound in the ear canal can be approximated quite well by a tube with a fixed diameter equal to that of the average adult ear canal. The tube is terminated at one end by a loudspeaker that delivers an acoustic signal in the frequency range up to at least 10,000 Hz. One may imagine that the air in the tube is partitioned into a very large number of infinitesimally thin discs (Beranek, 1949); each disc can be thought of as consisting of a layer of air particles. These discs of air are compressed or expanded by an applied force, such as a change in air pressure (air molecules will spread out from an area of high pressure to an area of lower pressure), and will return to their original volume once the applied force is removed.

Consider now what happens when the loudspeaker at one end of the tube generates an acoustic signal. When the speaker diaphragm moves

inward, it displaces and compresses the adjacent discs of air, which then displace and compress the next layer of air, and so on. By this means, the in and out movements of the transducer diaphragm create a pressure wave that travels down the tube at the speed of sound, about 343 m/s at 20°C. The velocity of each disc of air about its quiescent position (the position of the disc at rest) multiplied by its cross-sectional area is known as the *volume velocity*, as the product of velocity and cross-sectional area encompasses a moving volume.

The air in the tube opposes being displaced and compressed by the transducer diaphragm. The force exerted by the transducer diaphragm is equal to the pressure times the area of the diaphragm. The *work* done by the force is equal to force times the displacement, and is stored as energy in the air as it travels along the tube. The *acoustic power*,  $P(f)$  (the force times the volume velocity, often expressed in watts), inserted into the tube is equal to the rate of work done. The power propagated down the tube is transmitted without significant loss through the tube via the air.

TM. Impedance discontinuities result in frequency-dependent reflections of the sound wave, which we quantify using wideband reflectance.

The acoustic variables discussed in this section may be defined either in the time or frequency domain. It is important to always be aware of which

domain is under consideration. In this chapter, we work almost exclusively in the frequency domain, where all variables are functions of frequency,  $f$ . These variables are also a function of location. For measurements in the ear canal, we define  $x = 0$  as the measurement probe location and  $x = L$  the TM location.



## Pressure and Volume Velocity Waves

We denote the forward traveling pressure wave as  $P_+(f,x)$  [Pa], using the plus sign subscript to signify the forward direction (toward the TM). This wave is a function of both frequency  $f$  (in Hz) and location and has units of Pascals. Similarly, the reflected, backward traveling *retrograde* pressure wave is denoted  $P_-(f,x)$ . At any location in the ear canal, the total pressure  $P(f,x)$  is defined as

$$P(f,x) = P_+(f,x) + P_-(f,x). \quad (1)$$

The pressure is a scalar quantity (it has no direction). Any change in the pressure results in a force, which is a vector quantity (it has direction); this force leads to the motion (velocity) of air molecules in the direction of the force.

The corresponding acoustic *volume velocity*  $U(f,x)$  may be decomposed into forward  $U_+(f,x)$  and reverse  $U_-(f,x)$  traveling portions, as

$$U(f,x) = U_+(f,x) - U_-(f,x). \quad (2)$$

The volume velocity is a vector quantity, which accounts for the change in sign of Equation 2 (here positive  $U_-$  values indicate propagation of the retrograde wave toward the probe, and positive  $U_+$  values indicate propagation of the forward wave toward the TM).

The *complex acoustic reflectance*, which we represent using the uppercase Greek letter “Gamma,” is defined as the ratio of retrograde to forward traveling pressure (or velocity) waves

$$\Gamma(f,x) = \frac{P_-(f,x)}{P_+(f,x)} = \frac{U_-(f,x)}{U_+(f,x)}. \quad (3)$$

Since  $\Gamma(f,x)$  is complex, it may be expressed either as the sum of real and imaginary parts, or in terms of a magnitude and phase. The utility of the complex reflectance (as compared to other WAI quantities, such as impedance and admittance) is that the acoustic power is proportional to the square of the pressure. Thus, the squared magnitude of the reflectance describes the ratio of reflected to incident power (a value ranging between 0 and 1) as a function of frequency, while the reflectance phase codifies the latency of the reflected power (e.g., the depth at which the reflection occurs). Additionally, power absorbed by ear (potentially including the ear canal, middle ear, and inner ear) may be quantified as one minus the ratio of power reflected. The *power reflectance* at the probe may be defined as  $|\Gamma(f,0)|^2$ ; thus, the power absorbed by the ear is  $1 - |\Gamma(f,0)|^2$ . These properties of reflectance are more intuitive than impedance for formulating diagnoses of middle-ear pathologies.

For reference, the *complex acoustic impedance* is defined as the total pressure over the total volume velocity

$$Z(f,x) = \frac{P(f,x)}{U(f,x)}. \quad (4)$$

The *complex acoustic admittance* is given by  $Y(f,x) = \frac{1}{Z(f,x)}$  and various other WAI quantities may be calculated from  $Z(f,x)$  and  $Y(f,x)$ , as outlined in Appendix 1–A. This variety of immittance quantities can be confusing, so it is important to remember that they may all be derived from the complex acoustic reflectance. Specifically, the complex impedance is related to the reflectance via

$$Z(f,x) = r_0 \frac{1 + \Gamma(f,x)}{1 - \Gamma(f,x)}, \quad (5)$$